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# Reentrant superconductivity in proximity to a topological insulator


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MIEM, HSE

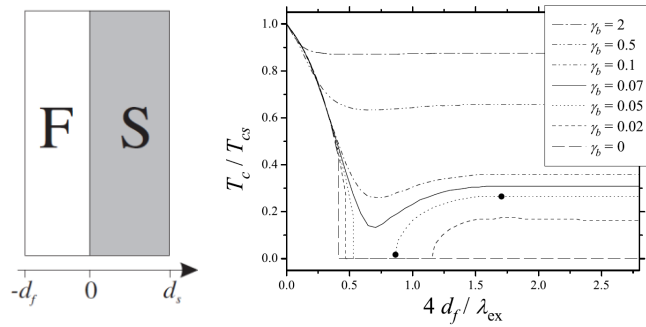
## Reentrant superconductivity in proximity to a topological insulator

T. Karabassov,<sup>1</sup> A. A. Golubov,<sup>2,3</sup> V. M. Silkin,<sup>4,5,6</sup> V. S. Stolyarov,<sup>3,7</sup> and A. S. Vasenko <sup>1,8,\*</sup>



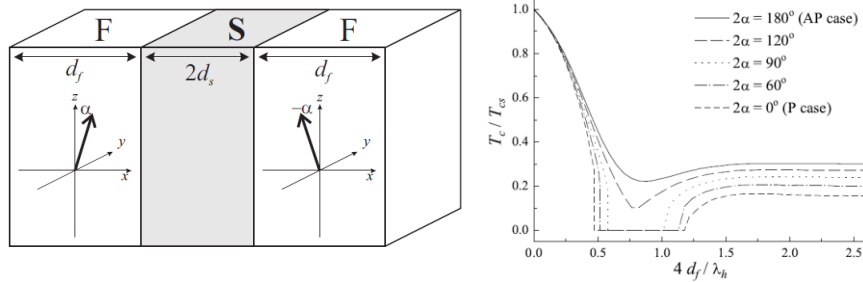


# Critical temperature in S/F systems

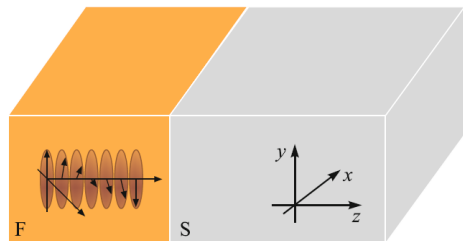


Khusainov, Proshin, PRB 56, 1997

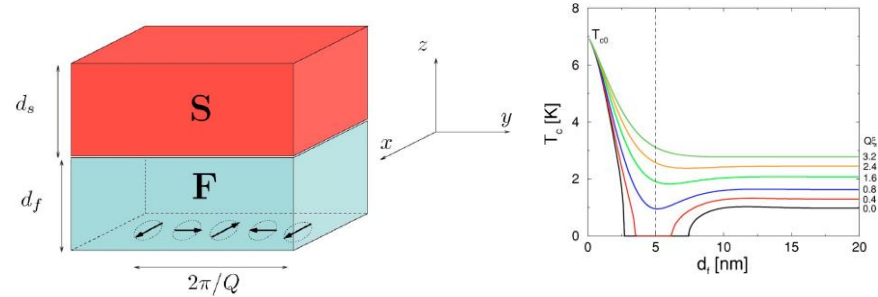
Fominov et al, PRB,2002



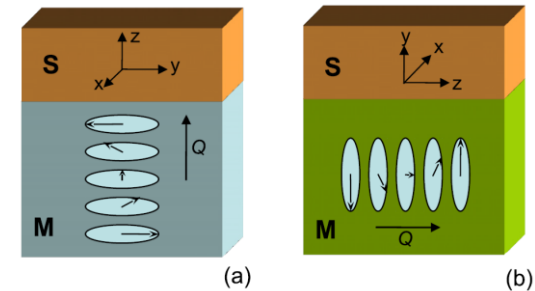
Fominov et al., JETP Lett, 2003



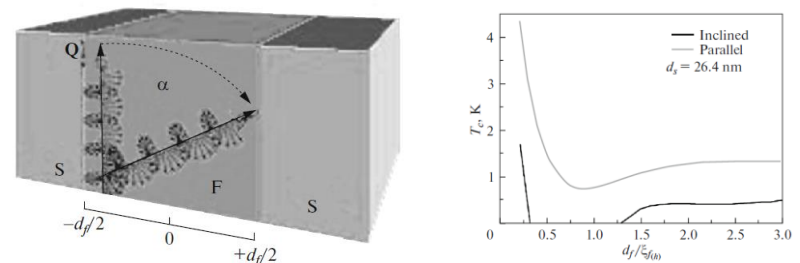
Pugach, Safonchik, JETP Lett, 2018



Champel, Eschrig, PRB,2005

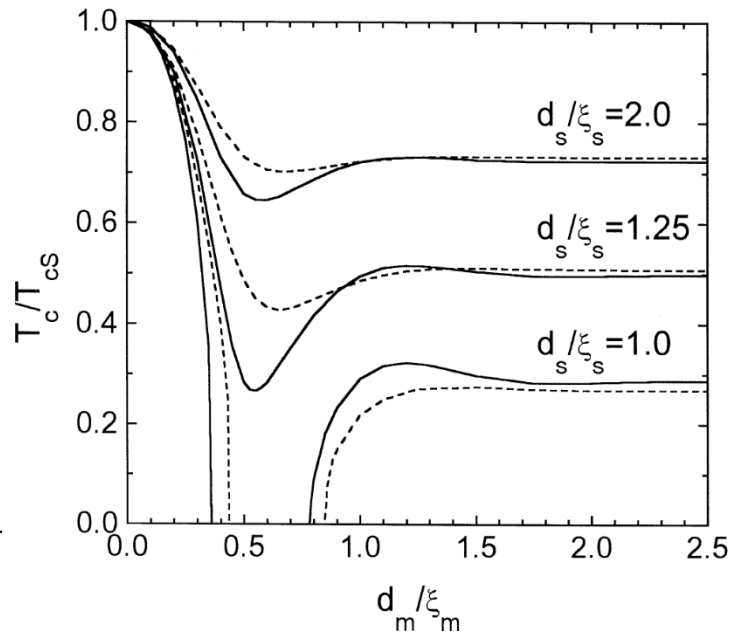
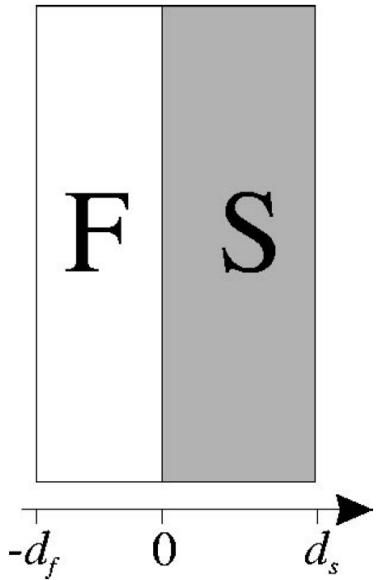


Pugach et al., APL, 2017

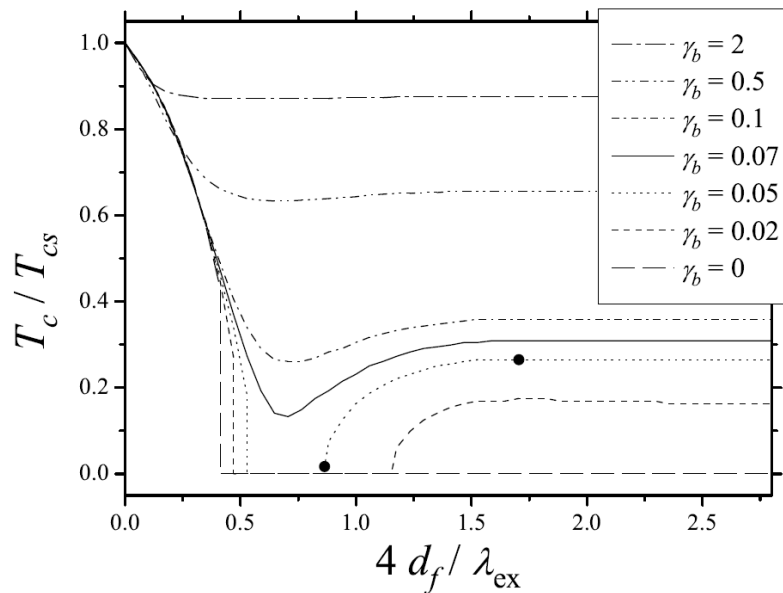


Pugach et al., Phys. Solid State, 2018

# Critical temperature in S/F bilayers

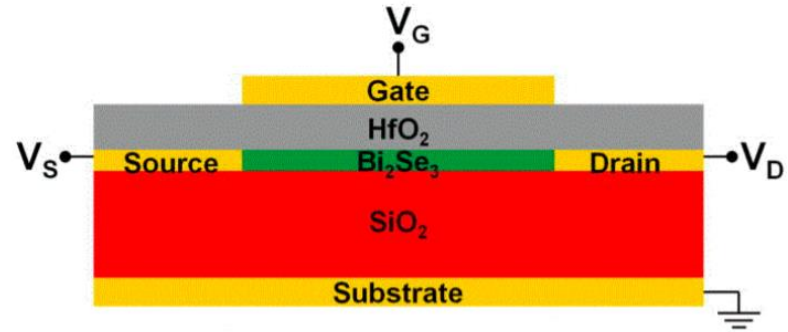
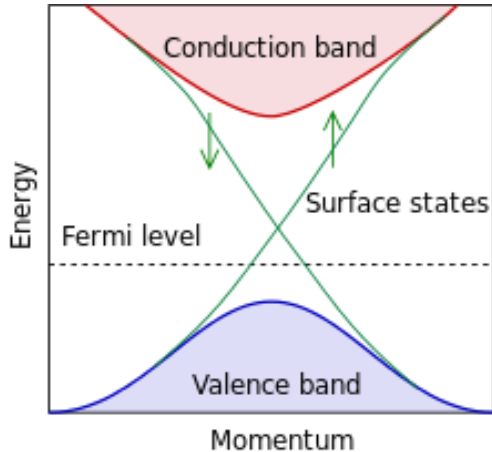


Khusainov, Proshin, PRB **56**,  
R14283(R) (1997)

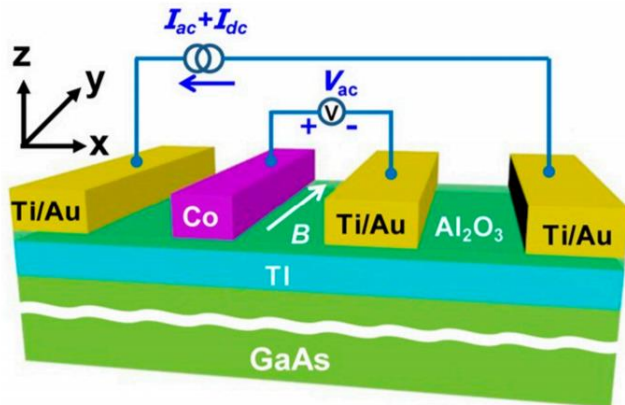


Fominov, Chtchelkatchev,  
Golubov, PRB **66**, 014507  
(2002)

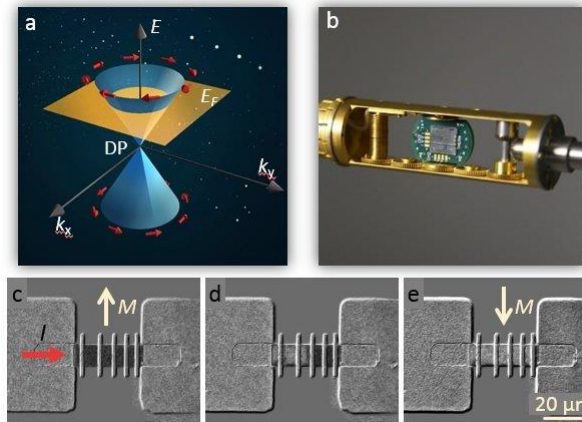
# Topological insulators



Chang et al. J. Appl. Phys., **112**, 124511 (2012)  
Field-effect Transistor



Tang et al. Nano Lett., **14**, 5423 (2014)  
Detector of Spin-Polarized Surface States

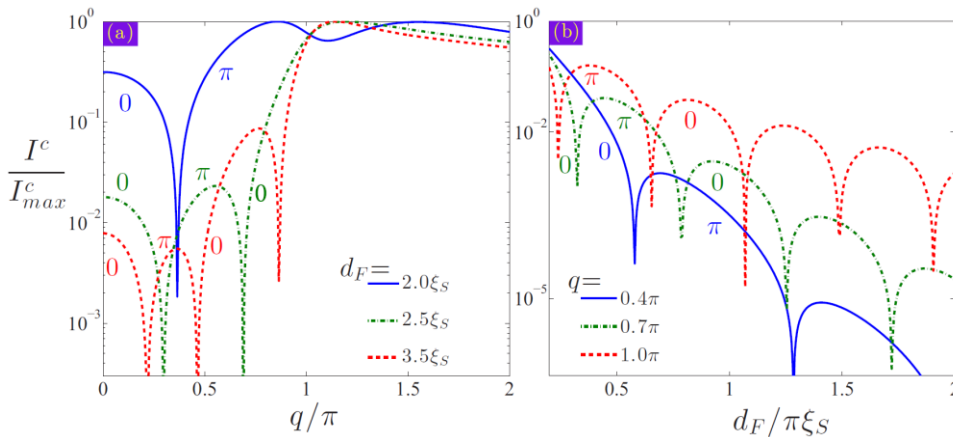
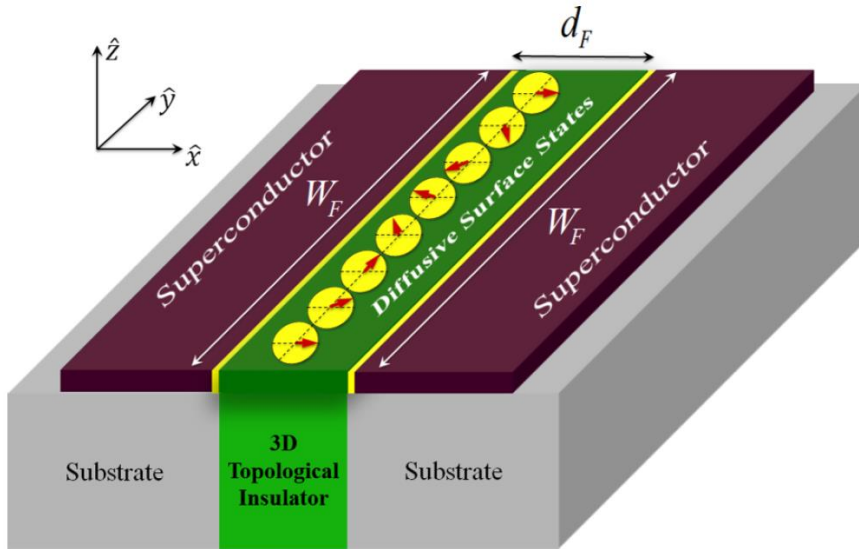


Wang et al., Nat. Commun. **8**, 1364 (2017)  
Spin-Orbit Torques for Spintronic applications

# Josephson junction through a disordered topological insulator with helical magnetization

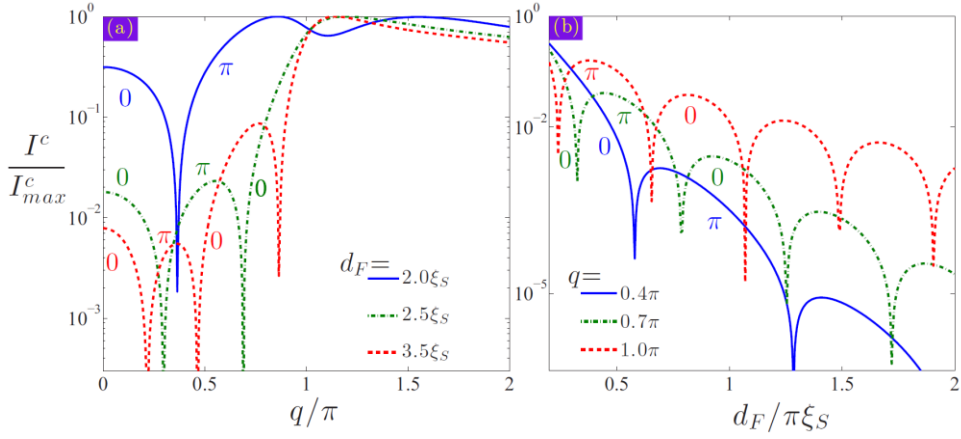
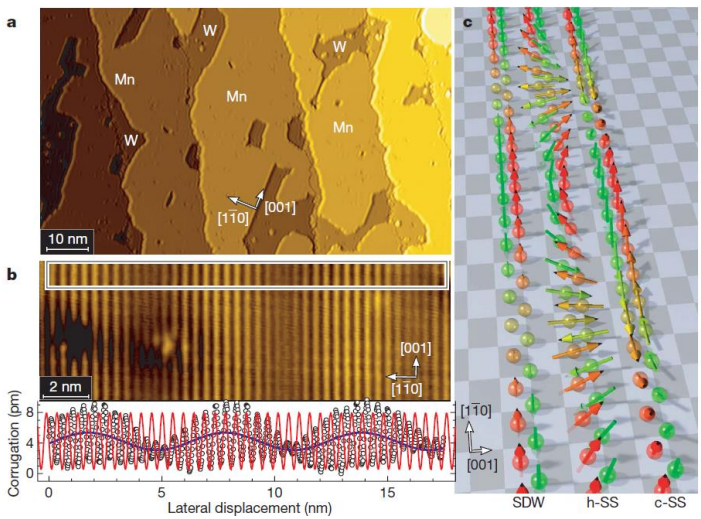
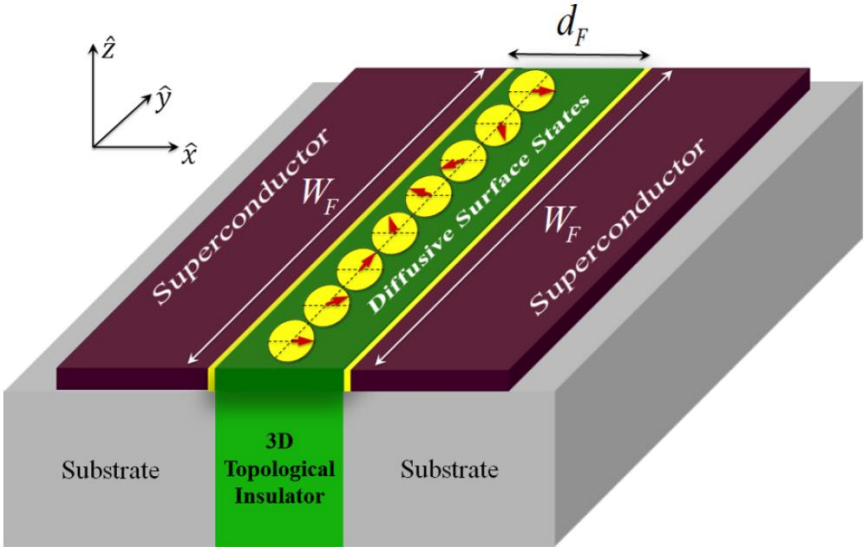
Alexander Zyuzin, Mohammad Alidoust, and Daniel Loss

*Department of Physics, University of Basel, Klingelbergstrasse 82, CH-4056 Basel, Switzerland*



# Chiral magnetic order at surfaces driven by inversion asymmetry

M. Bode<sup>1†</sup>, M. Heide<sup>2</sup>, K. von Bergmann<sup>1</sup>, P. Ferriani<sup>1</sup>, S. Heinze<sup>1</sup>, G. Bihlmayer<sup>2</sup>, A. Kubetzka<sup>1</sup>, O. Pietzsch<sup>1</sup>, S. Blügel<sup>2</sup> & R. Wiesendanger<sup>1</sup>

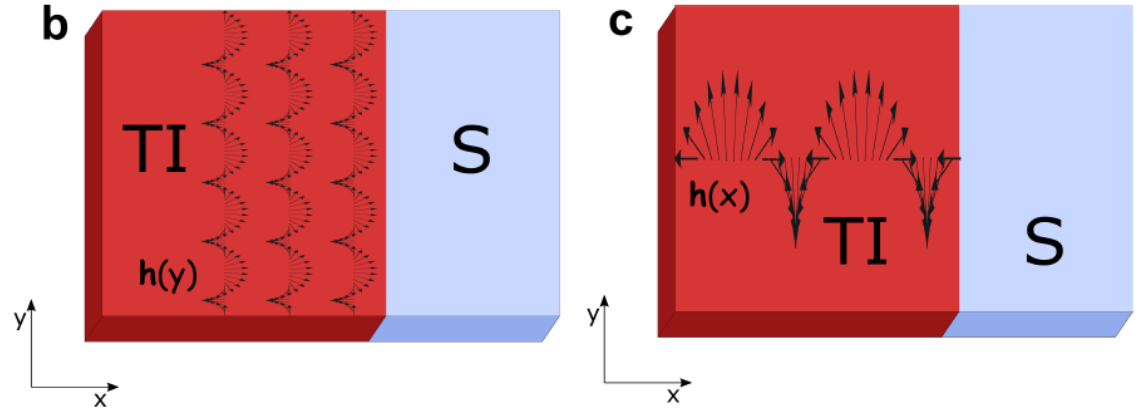
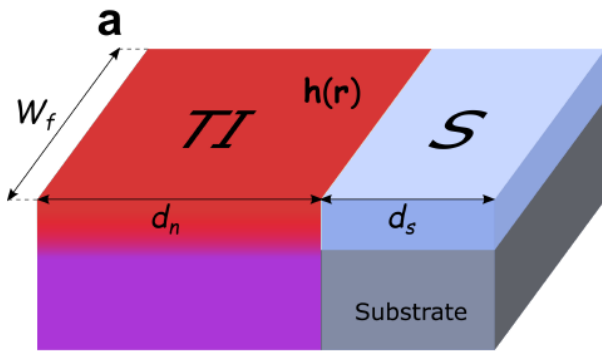


manganese on a tungsten substrate  
 Bode et al., Nature, **447**, 191 (2007)



# Our model

## Superconductor/Topological insulator with induced magnetization



*Helical magnetization*  
 *$\mathbf{h}$  in x-y plane*

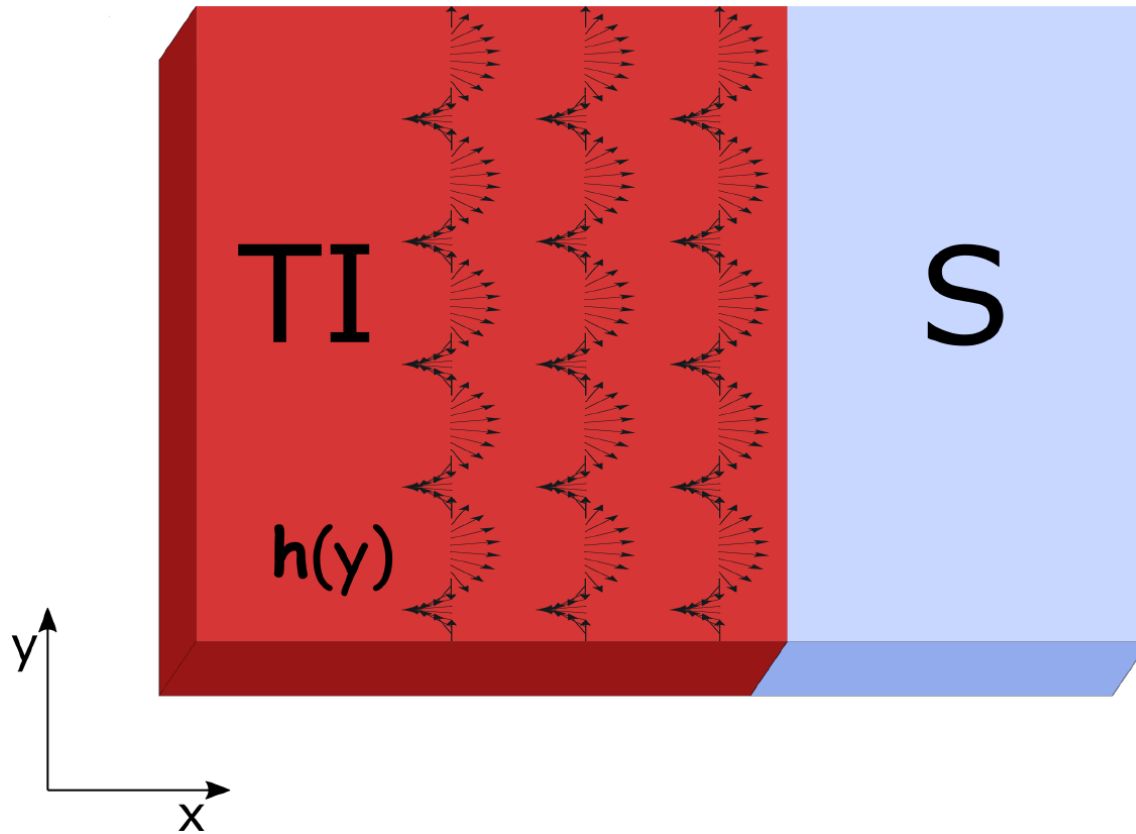
$$\mathbf{h}(y) = h_0(\cos Qy, \sin Qy, 0) \quad (1)$$

$$\mathbf{h}(x) = h_0(\cos Qx, \sin Qx, 0) \quad (2)$$

$$Q = \frac{2\pi}{\lambda}$$

# Helical magnetization $\mathbf{h}(y)$

$$\mathbf{h}(y) = h_0(\cos Qy, \sin Qy, 0)$$



$$Q \gg 1$$

# Theoretical model

A. Zyuzin, M. Alidoust, and D. Loss, PRB, 2016

$$\xi_s^2 \pi T_{cs} \left( \frac{d^2}{dx^2} + \frac{d^2}{dy^2} \right) f_s - |\omega_n| f_s + \Delta = 0$$



$$\Delta \ln \frac{T_{cs}}{T} = \pi T \sum_{\omega_n} \left( \frac{\Delta}{|\omega_n|} - f_s \right)$$

$$\begin{aligned} & \left( \frac{\partial}{\partial x} - \frac{2i}{\alpha} h_y(y) \right)^2 f_T + \left( \frac{\partial}{\partial y} + \frac{2i}{\alpha} h_x(y) \right)^2 f_T \\ & = \frac{|\omega_n|}{\xi_n^2 \pi T_{cs}} f_T \end{aligned}$$

$$2\gamma \hat{g}_s \mathbf{n} \cdot \hat{\nabla} \hat{g}_s = [\hat{g}_s, \hat{g}_{SC}]$$

S

TI

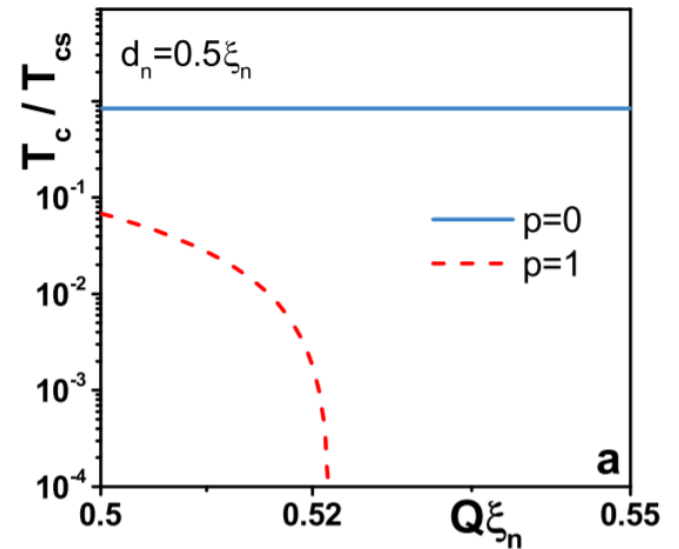
# Theoretical model

$$f_T(x, y) = \sum_{p=-\infty}^{+\infty} f_T^{(p)}(x) e^{ipQy}$$

$$f_s(x, y) = \sum_{p=-\infty}^{+\infty} f_s^{(p)}(x) e^{ipQy}$$

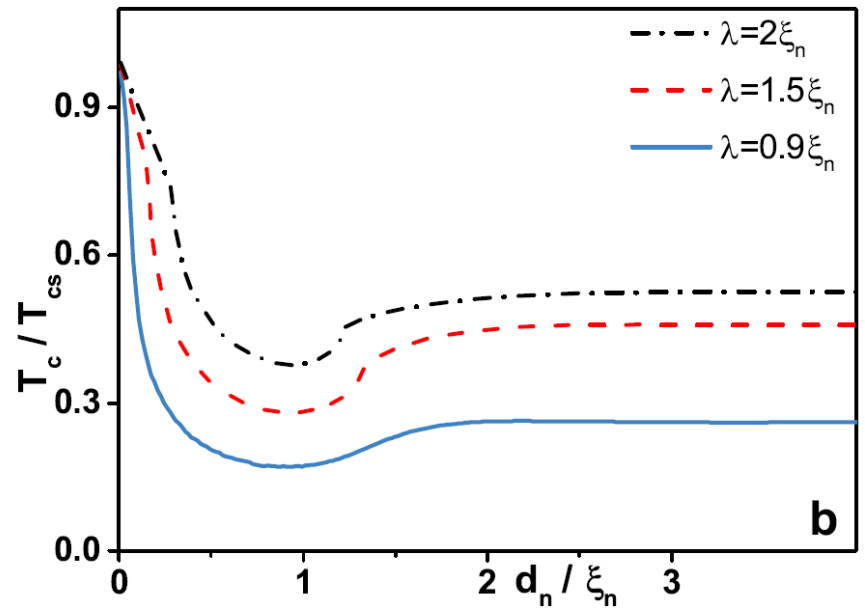
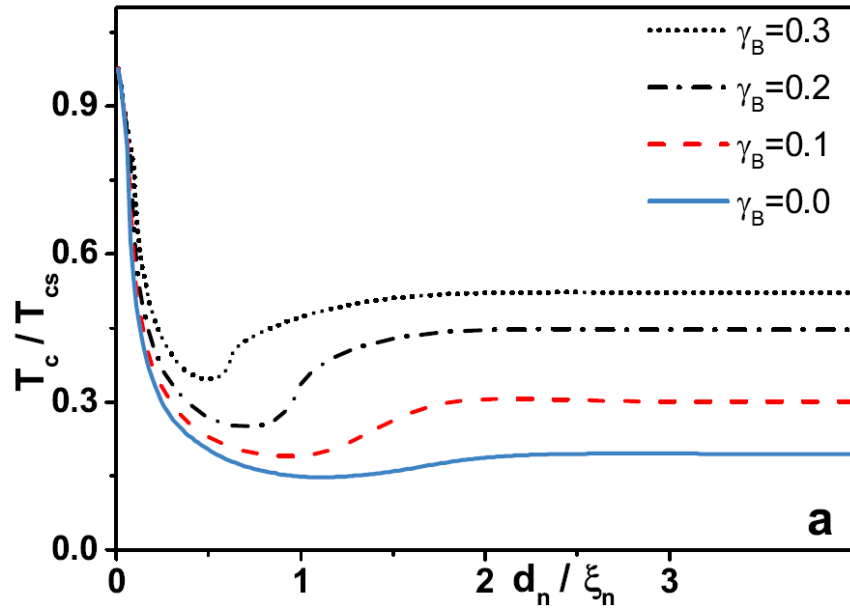
$$\Delta(x, y) = \sum_{p=-\infty}^{+\infty} \Delta^{(p)}(x) e^{ipQy}$$

$Q \gg 1$





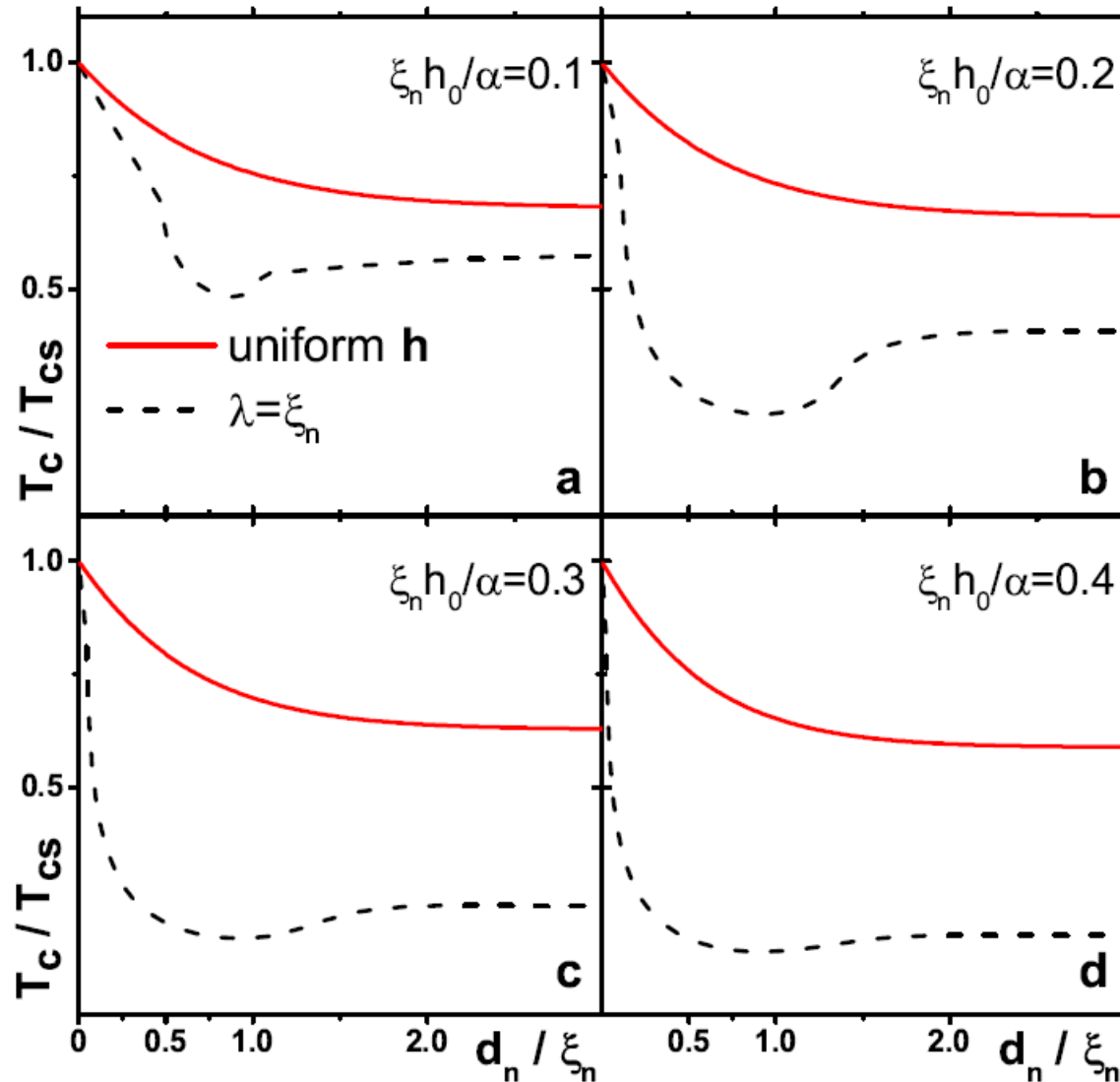
# Helical magnetization $h(y)$



$$\gamma_B = R_b \sigma_n / \xi_n$$

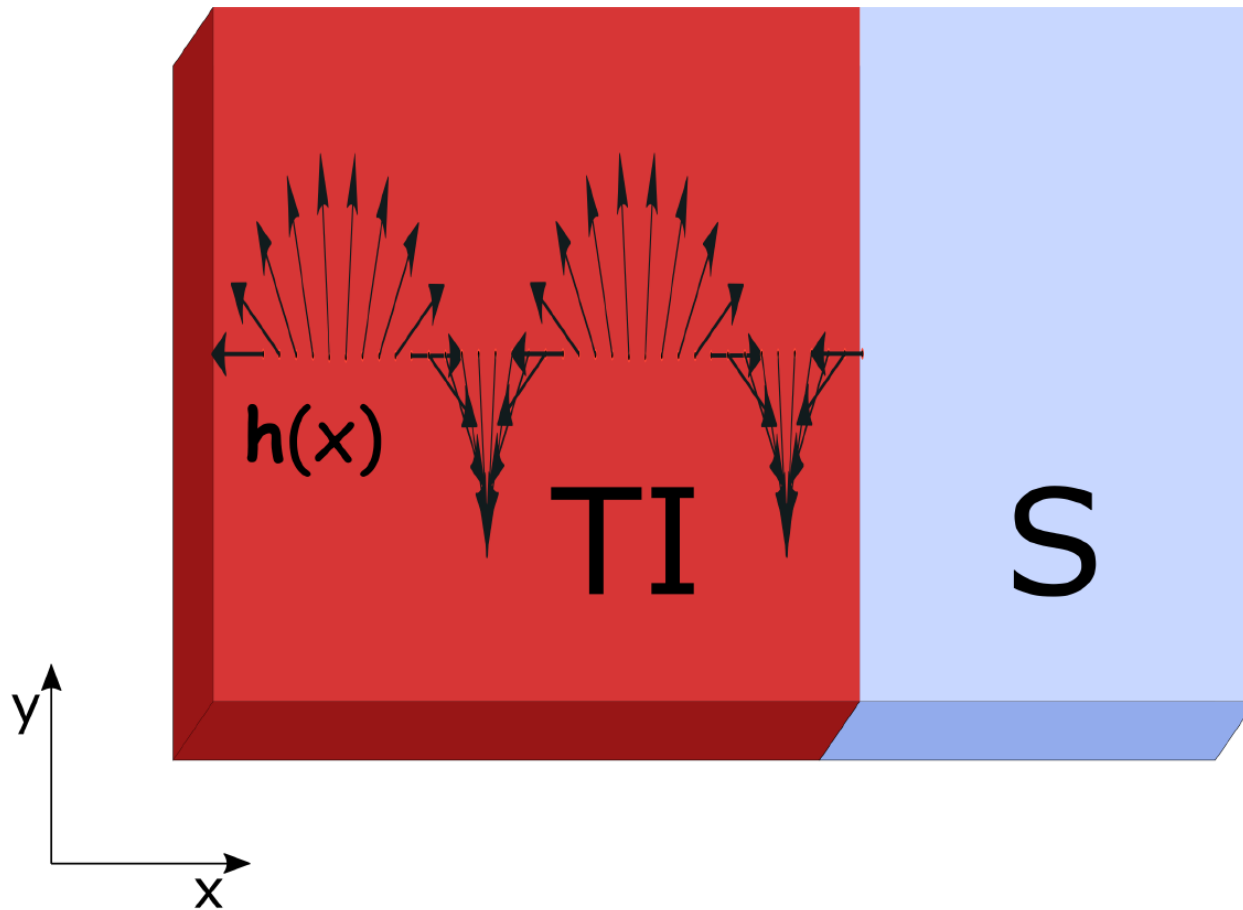
$$Q = \frac{2\pi}{\lambda}$$

# Comparison with uniform exchange field



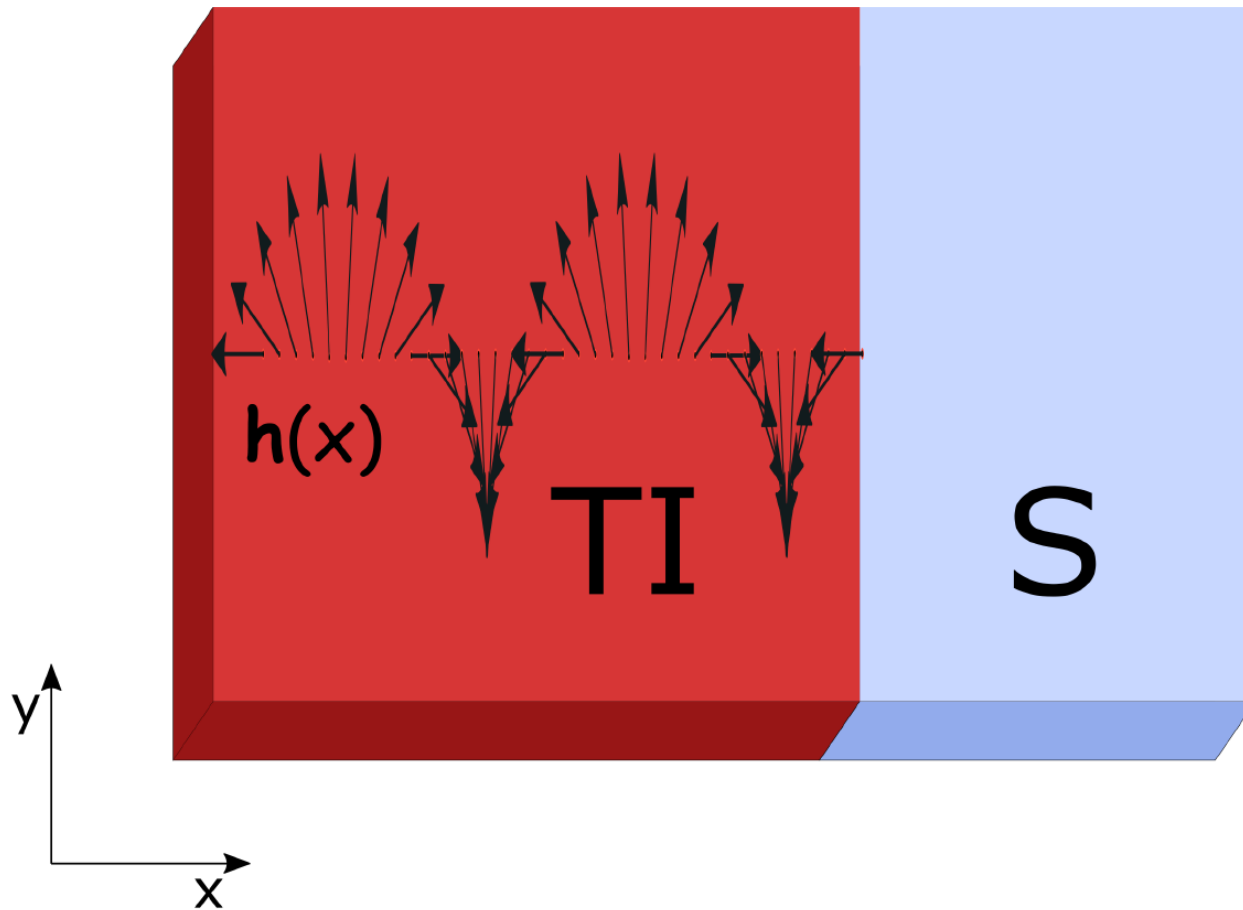
# Helical magnetization $\mathbf{h}(x)$

$$\mathbf{h}(x) = h_0(\cos Qx, \sin Qx, 0)$$



# Helical magnetization $\mathbf{h}(x)$

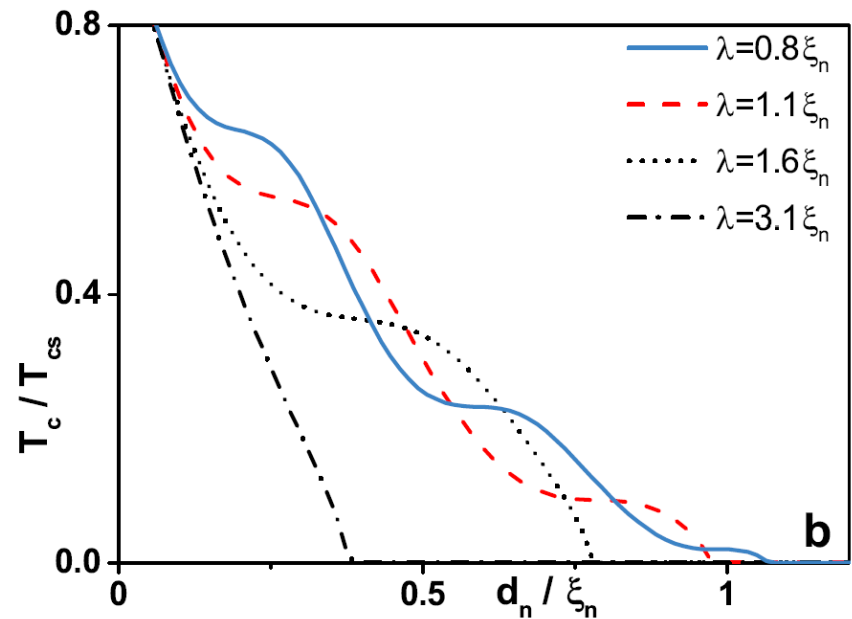
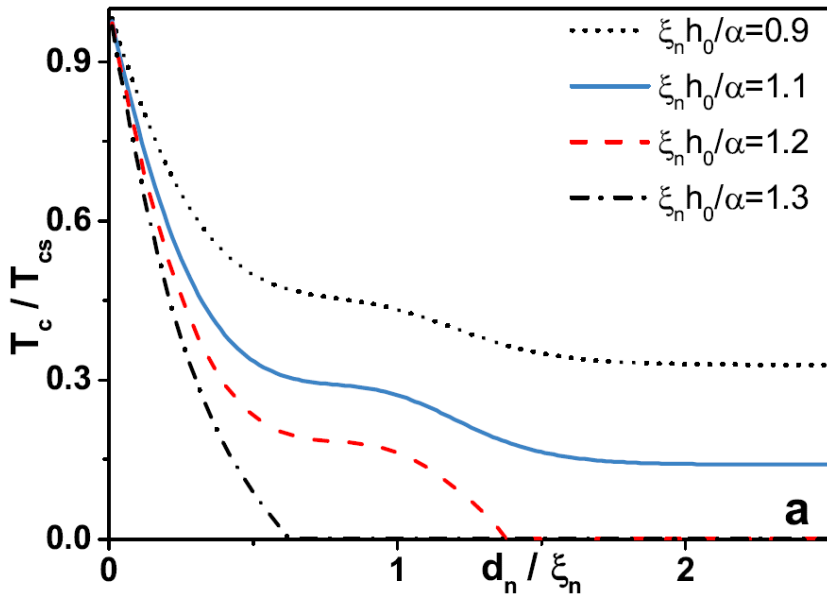
$$\mathbf{h}(x) = h_0(\cos(Qx + \phi_0), \sin(Qx + \phi_0), 0)$$





# Helical magnetization $\mathbf{h}(x)$

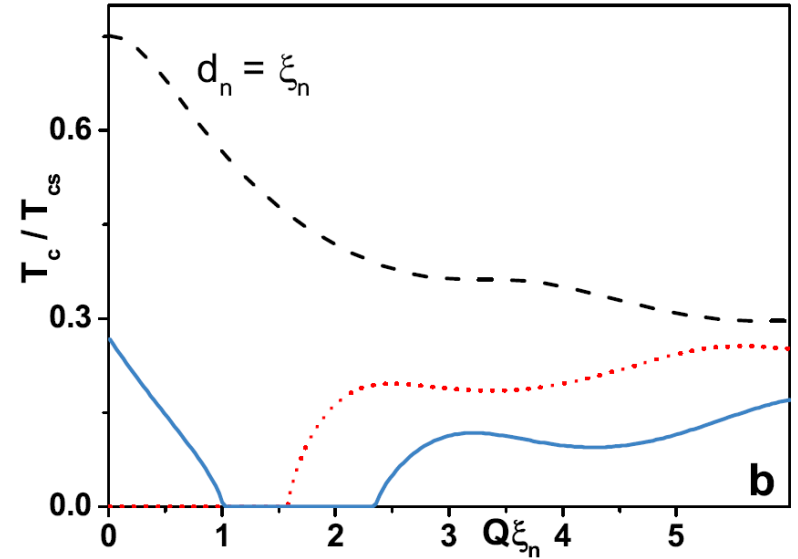
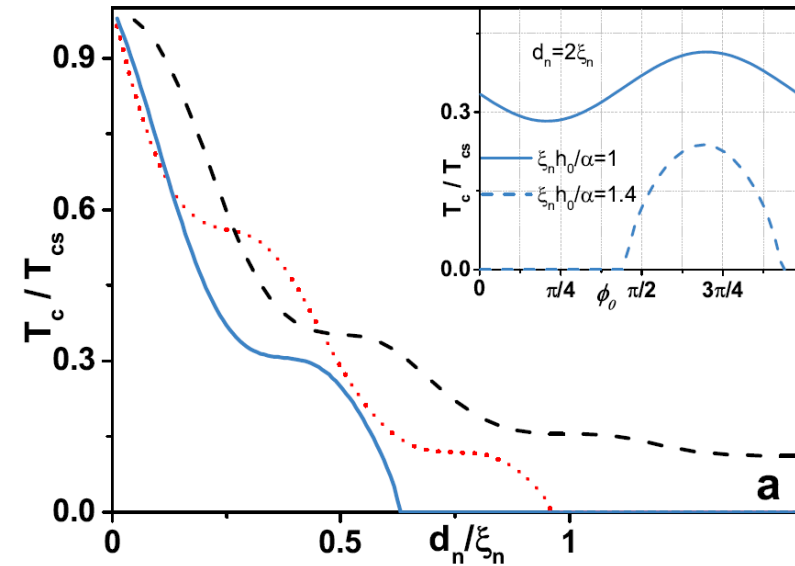
$$\mathbf{h}(x) = h_0(\cos(Qx + \phi_0), \sin(Qx + \phi_0), 0)$$



$$\phi_0 = 0$$

# Helical magnetization $\mathbf{h}(x)$

$$\mathbf{h}(x) = h_0(\cos(Qx + \phi_0), \sin(Qx + \phi_0), 0)$$



.....  $\phi_0 = 0$ , ———  $\phi_0 = \pi/4$ , - - -  $\phi_0 = \pi/2$

# Summary

- A model for calculating the critical temperature in the S / TI hybrid structure has been developed;
- We found monotonic dependence of  $T_c$  for uniformly magnetized TI;
- Non-monotonic behavior of  $T_c$  for helical magnetization pattern was revealed.

# Thank you!